A CONTRIBUTION TO RESEARCH OF DEGRADATION OF CHARACTERISTICS OF VIBRATION PARAMETERS ON VIBRATION ASPECT OF VEHICLE COMFORT

Dr Miroslav Demić *
University of Kragujevac, Faculty of Engineering Science, Kragujevac, Serbia
Dr Đorđe Diligenski
Vinča Institute of Nuclear Sciences, Department of Motor Vehicles and IC engines, Belgrade, Serbia

Dynamic simulation, based on modeling, has a significant role in vehicle development, especially in the early stages of design process, when relevant parameters are being defined. In praxis it is usually assumed that vibration parameters are unchangeable, what is basically wrong. All researches indicate that vibration parameters degrade in time of vehicle service, consequently leading to a variation of its dynamic characteristics. This paper, based on preliminary research results, attempts to point out the necessity of taking into consideration this variation in the earliest phases of vehicle design by its implementation in the vehicle simulation model.

Key words: Vehicle, Vibration parameters, Degradation, Vibration comfort

INTRODUCTION

Dynamic simulation has important role in development of motor vehicles, based on modeling, by use of application of numerous vehicle models [05-16,22,24-26,28,29]. It can be assumed that the mechanical model, in the general form, is described by the equation [05, 06]:

$$\dot{Z} = \dot{Z}(Z, A, U, L, Q, t) \qquad (1)$$

where:

- Z - vector of generalized coordinates of the vibration system,
- A - vector of vehicle vibration parameters,
- U - vector of control functions,
- Q – time function of excitation (coming from road microprofile, engine function, unbalanced masses, tire nonuniformities, etc.),
- L – function that takes into account stochastic variation of characteristics of vibration parameters during the vehicle service life, and
- t - time.

General solution of vector differential equation (1) can be written in the form [05-06]:

$$Z = Z(A, U, L, t) \qquad (2)$$

The simplest case is when there does is no control function (U=0) and when variation of vibration parameters of a vehicle in service is not taken into account (L=0), i.e.:

$$Z = Z(A, t) \qquad (3)$$

In practice, a simplification given by expression (3) is commonly used, which neglects the influence of duration of service time on variation of vehicle vibration parameters. However, it represents a major simplification, according to [23], where the existence of the mentioned variation is shown. Therefore, this problem will be considered in details by application of the appropriate vehicle vibration model.

SELECTION OF VEHICLE VIBRATION MODEL

The structure of a vehicle model is chosen with regard to the variables supposed to be analyzed [04, 05]. Therefore, vibration model of various structure and complexity [05-16,20-22,24-31]. The vehicle model should be chosen to be as simple as possible, and to enable simulation of the desired value [05,06]. A vehicle vibration model, often regarded in literature as quarter

model [21,22,24,26,28,29], given in Figure 1, has been estimated to be optimal for the observation, bearing in mind that the aim of this research was to introduce degradation of vibration parameters in the model.
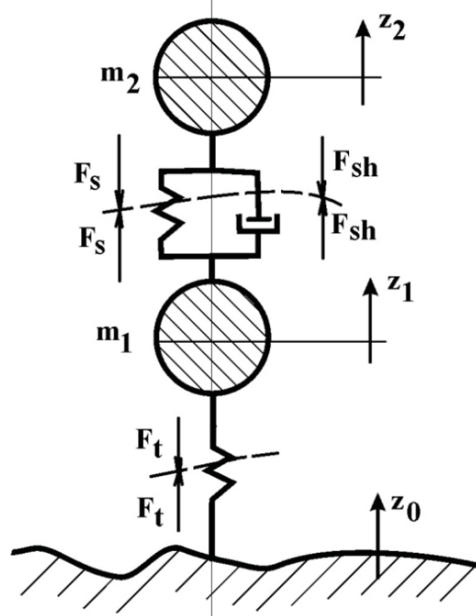

Figure 1: The equivalent vehicle model

Where the following signs were applied:

- m_1, m_2 –unsprung and sprung mass of quarter vehicle model, respectively (in this case 27.5 and 250 kg),
- Fs – force in the spring,
- Fsh – force in the shock absorber, and
- Ft – force in the tire.

Force in the tire can be represented by the polynomial equation of the third degree [05-15, 20,21,23,25]:

$$F_{op} = c_1 \Delta z + c_2 \Delta z^3 \qquad (4)$$

where:

- c_1 and c_2 – stiffness parameters, and
- Δz – spring relative deformation.

Force in the shock absorber depends not only on the relative speed but on the relative motion and acceleration [01, 16]. The analyses have shown that the model defined in [01, 16], which applies transcendent functions of acceleration, can hardly be used in modeling of vehicles with more than one degree of freedom. That comes from the fact that the acceleration is covered by the function tangens hyperbolicus, in which case problems of decoupling of differential equations

of motion, for model with two or more degrees of freedom of motion. Besides, it appears that the acceleration is of minor influence on the force than displacement and velocity, so for further analyses a model [01, 16] has been adopted, where the force is described with the expression:

$$F_{sh} = \{x_1 + x_{2,3} \cdot \Delta\dot{z} + x_4 \cdot \Delta\dot{z}^2 sign(\Delta\dot{z})\} \cdot$$
$$\cdot \{x_5 + x_6 \quad \cdot th(\frac{\Delta z}{3 \cdot \sigma_{\Delta z}})\} \qquad (5)$$

where:

- Δz and $\Delta\dot{z}$ - relative displacement and velocity, respectively, and
- x_1, $x_{2,3}$, x_4, x_5 and x_6 – parameters of shock absorber model.

Radial force in the tire is also nonlinear [20,21,23,25], and therefore the following expression is used:

$$F_p = c_3\Delta + c_4\Delta^2 + c_5\Delta^3 \qquad (6)$$

where:

- Δ -radial deformation of the tire, and
- c_3, c_4 and c_5 – parameters of tire radial stiffness.

As it is well known, vertical vehicle vibration depend on type of road, velocity and the number of passengers riding in the vehicle. Having that in mind, the analysis is performed for the case that there are two passengers in the vehicle, riding with the characteristic velocity of 30 m/s [32] on a good asphalt road, whose time excitation function is shown in Figure 2 [16]. To be more precise, a polyharmonic excitation function is applied because the analyses have shown that it represents a good approximation of real road microprofile, for the applied vehicle velocity of 30 m/s.

Bearing in mind the observed vehicle vibration model, by use of Newton's law [27,31], the following differential equations of vibration motion of vehicle are obtained:

$$m_1\ddot{z}_1 = F_s + F_{sh} - F_t \qquad (7)$$
$$m_2\ddot{z}_2 = -F_s - F_{sh} \qquad (8)$$

where:

- $\ddot{z}_1$, $\ddot{z}_2$ -accelerations of unsprung and sprung mass measured from the equilibrium position, respectively,
- Fs – force in the spring given by expression (4),

- F_{sh} – force in the shock absorber given by expression (5), and
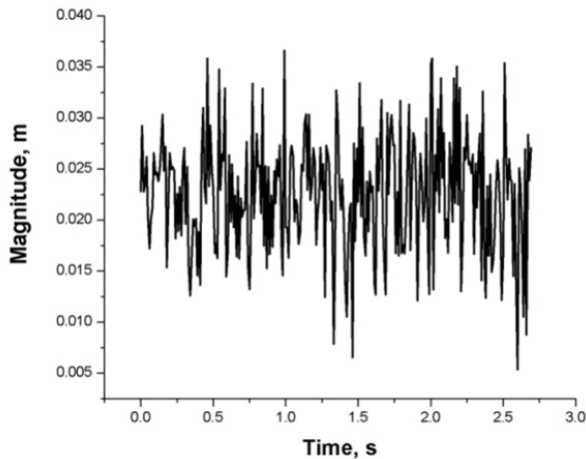- F_t – radial force in the tire given by expression (6).

Figure 2: The applied function of road microprofile excitation for the velocity of 30 m/s

Bearing in mind nonlinear and very complex structure of expressions (4,5,6), even in case of such a simple vehicle model, as well as quasis-tochastic character of the excitation function, it appears to be obvious that the vehicle model described by equations (8,9) is complex and cannot be solved in finite form.

The analyses have shown that the argument of the tangens hyperbolicus function in the expression (5) – displacement divided with the triple variation – lies in the domain -1.8 to +1.8 (established on the basis of the experimental results [01, 15].

It can be noted that the argument of the observed function is usually in the interval -1 to +1, and the relative error of approximation of the mentioned function with the Maclaurin polynomial of third degree is approx. 9% [01,16], which is found acceptable.

During the simulation, parameters of the passenger car "Zastava 1100" were utilized, provided by the manufacturer [32], and shown in Table 1.

Table 1: Vehicle parameters

c_1, N/m	c_2, N/m^3	c_3, N/m	c_4, N/m^2	c_5,N/m^3
50000	10000	5000	500000	500000
x_1, 1/N	x_2./x_3, s/s	x_4, s$_2$/m	x_5, N/m	x_6, N/m
20.25	0.008/0.02	-9.51	-2.091	0.0015

It should be pointed out that dimensions of the coefficients in Table 1 are within SI unit system.

METHOD

Parameters of elasto-damping elements are variable values during the service life. To be more precise, their values tend to descend. For the illustration, Figure 3 shows a typical example of that variation [23], where it is assumed that values of parameters descend linearly with the duration of service, expressed in km. Data from Figure 3 enable analysis of the influence of vibration parameters variation on vehicle dynamic characteristics.
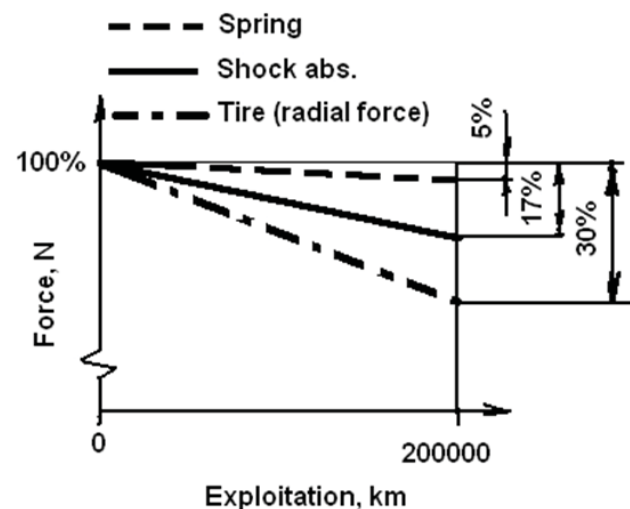

Figure 3: Variation of vibration parameters in service

For the analysis of the influence of vehicle dynamic cahracteristics due to variation of parameters of elasto-damping elements in service, two groups of parameters were utilized, taking into account these variations. To be more precise, having in mind Figure 3, after approximation with streight line, any variation is described by the expression:

$$vibpar(\tau)=vibpar_0 \cdot k_i \qquad (9)$$

where:

- $vibpar(\tau)$ – value of vibration parameter after service of (τ) kilometers,
- $vibpar_0$ - value of vibration parameter at the beginning of vehicle service, and
- k_i – factor that takes into account degradation of vibration parameters during service.

In order to take into account the influence of aging on vehicle dynamic characteristics, on the basis of the data given in Figure 3, corrective parameters are adopted and given in Table 2. It should be pointed out that factor k_1 refers to

springs, k_2 to shock absorbers and k_3 to tires, and there were two groups of factors observed: at the beginning of service (group 1) and after 200000 kilometers of service (group 2).

As it has already been pointed out, differential equations (7,8) are solved numerically, by use of method Runge-Kutta, with the sample of increment 0.01s, in 1024 points, which enabled reliability of the results within the domain 0.1–50 Hz, what is regarded acceptable for this kind of analysis [02-04, 13-15].

On the basis of [02-04], statistical values of errors were calculated. For the signal of 1024 points with the sample of increment 0.01, number of averaging 256, bias errors were obtained 0.003, stochastic error for a single signal 0.10, and for two signals 0.118, for spectra. Such small values of errors indicate that these results enable reliable analyses.

Table 2: Corrective factors

	k_1	k_2	k_3
Group 1	1	1	1
Group 2	0,95	0,83	0,70

ANALYSIS OF THE RESULTS

On the basis of the calculated time series of vertical vibration of sprung mass, ordinary coherence functions, cross-correlation functions and transfer functions for the initial state were calculated, and also for the state of vibration parameters after 200000 km of service, by use of software [17, 18], and presented in Figures 4-7.
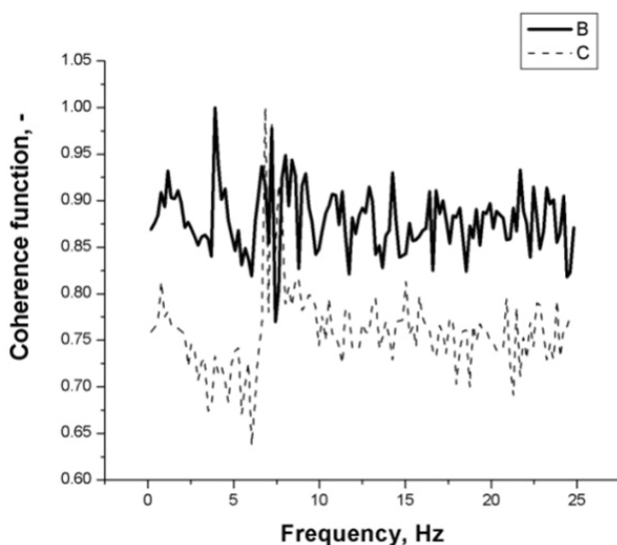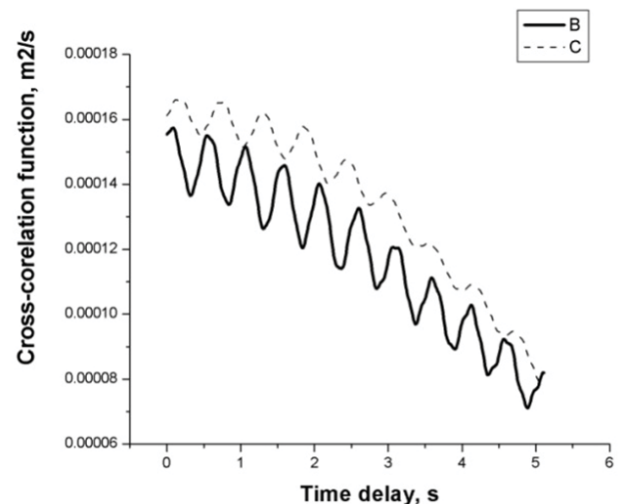

Figure 5: Cross-correlation function

The analysis of the data from the Figure 4 may lead to the conclusion that ordinary coherence function is subject to variation within the interval 0.65 – 1, what indicates that the vehicle model is nonlinear [02-04]. Degradation of vibration parameters also influences the value of ordinary coherence function.

Figure 5 presents the variation of cross-correlation function with the increment of time duration. To be more precise, it descends with the time increment and gravitates towards zero value, and also indicates that the process of vibration is stationary, what is understandable when the applied function of excitation is stationary value [02-04]. As in previous case, degradation of vibration parameters influences forced vibration of vehicle sprung mass.
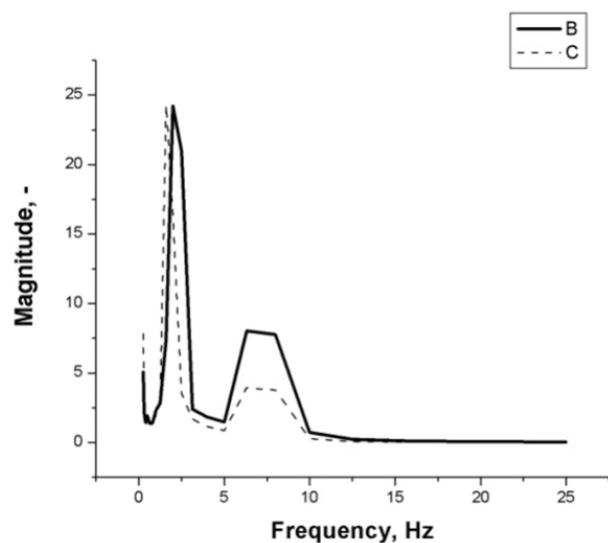

Figure 4: Ordinary coherence function

Figure 6: Modulus of transfer function

The analysis of data from the Figure 6 shows the resonance of sprung mass at approx. 2.5 Hz, and unsprung mass at approx. 7.5 Hz, which confirms the fact that vehicle parameters are well chosen [21]. It is obvious that degradation of vibration parameters leads to a variation of parameters of resonance of sprung and unsprung masses. I.e., since spring and shock absorber cahracteristics descend with the duration of service, it is clear that reduced damping leads to a variation of transfer function amplitude [26]. Variation of vibration parameters also influences the variation of phase angle, Figure 7.
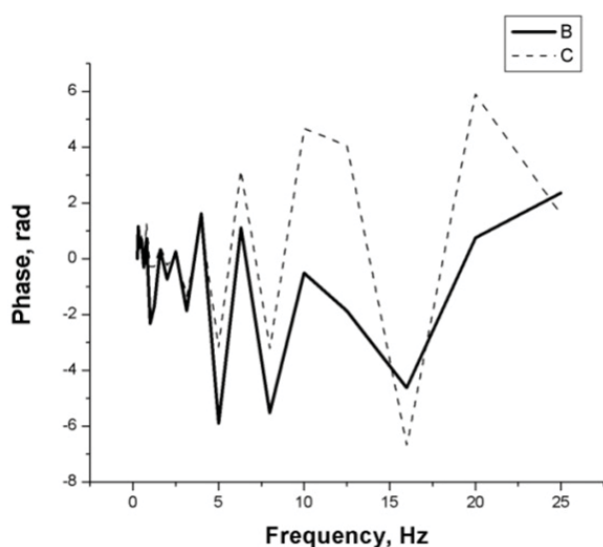

Figure 7: Phase angle of transfer function

It should be noticed that the variation of parameters of resonant point strongly influences parameters of vibration comfort of the vehicle, and degradation of these parameters may lead to a distraction of the vehicle due to unconfortable ride [12-14, 18]. This effect is often noticed in service when shock absorbers are worn, or suspension characteristics degrade to the extent that makes the vehicle unsafe to use. Therefore, it appears to be a need to introduce a degree of the allowed degradation of vibration parameters, what is not the subject of this paper. It is important to point out that the influence of degradation of vibration parameters should be taken into consideration in the process of creating a vehicle model in the early phase of vehicle design.

CONCLUSIONS

Performed research enabled following conclusions:

- Degradation of vibration parameters during the service influences the variation of characteristics relevant for vehicle vibration comfort.
- The influence of degradation of vibration parameters should be taken into account in vehicle model in the early phase of vehicle design

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